

1. $\frac{a+1}{-3} = \frac{-2}{1} \Leftrightarrow a = 5$

Opção (B)

2.

2.1 $\overline{AB} + \overline{BC} = \overline{AC} = C - A = (-1, 0) - (2, -3) = (-3, 3)$

$$\|\overline{AB} + \overline{BC}\| = \|\overline{AC}\| = \sqrt{(-3)^2 + 3^2} = 3\sqrt{2}$$

2.2. $M = \left(\frac{2+2}{2}, \frac{-3-1}{2}\right) = (2, -2)$

$$\overline{CM} = M - C = (2, -2) - (-1, 0) = (3, -2)$$

$$4\overline{CM} - \vec{u} = 4(3, -2) - (4, -3) = (12, -8) - (4, -3) = (8, -5)$$

$$\overline{BP} = P - B = (x, y) - (2, -1) = (x-2, y+1)$$

$$\overline{BP} = 4\overline{CM} - \vec{u} \Leftrightarrow \begin{cases} x-2 = 8 \\ y+1 = -5 \end{cases} \Leftrightarrow \begin{cases} x = 10 \\ y = -6 \end{cases}$$

$$P(10, -6)$$

2.3. $\vec{v} = k\vec{u} = k(4, -3) = (4k, -3k), k \in \mathbb{R}$

$$\|\vec{v}\| = 10 \Leftrightarrow \sqrt{(4k)^2 + (-3k)^2} = 10 \Leftrightarrow \sqrt{25k^2} = 10 \Leftrightarrow 25k^2 = 100 \Leftrightarrow k^2 = 4 \Leftrightarrow$$

$$\Leftrightarrow k = 2 \vee k = -2$$

Como \vec{v} tem sentido contrário ao de \vec{u} , $k < 0$, então $\vec{v}(-8, 6)$.

3.

3.1. $-3x - 2y + 5 = 0 \Leftrightarrow y = -\frac{3}{2}x + \frac{5}{2}$

\vec{r} é colinear com $\vec{v}(2, -3)$.

Então, $\vec{r}(6, -9)$.

Opção (D)

3.2. $m = -\frac{1}{2}$

$$y = -\frac{1}{2}x + b, \text{ então } 1 = -\frac{1}{2} \times 4 + b \Leftrightarrow b = 3$$

$$s: y = -\frac{1}{2}x + 3$$

3.3. $B(0, 3)$

$$-\frac{1}{2}x + 3 = 0 \Leftrightarrow x = 6, \text{ então } A(6, 0).$$

$$A = \frac{6 \times 3}{2} = 9 \text{ u.a.}$$

4. $\overline{AB} = B - A = (x, 0, 0) - (0, y, 0) = (x, -y, 0)$

Opção (D)

5.

5.1. $\overline{AB} = B - A = (6, 0, 4) - (3, 6, 2) = (3, -6, 2)$

$$F = E + \overline{AB} = (1, 3, -4) + (3, -6, 2) = (4, -3, -2)$$

5.2. $\overline{AE} = E - A = (1, 3, -4) - (3, 6, 2) = (-2, -3, -6)$

$$(x, y, z) = (3, 6, 2) + k(-2, -3, -6), \quad k \in \mathbb{R}$$

$$(x, y, 0) = (3, 6, 2) + k(-2, -3, -6), \quad k \in \mathbb{R} \Leftrightarrow$$

$$\Leftrightarrow \begin{cases} x = 3 - 2k \\ y = 6 - 3k \\ 0 = 2 - 6k \end{cases} \Leftrightarrow \begin{cases} x = \frac{7}{3} \\ y = 5 \\ k = \frac{1}{3} \end{cases}, \text{ então } P\left(\frac{7}{3}, 5, 0\right).$$

5.3. $\overline{AD} = \overline{AB} = \overline{AE} = \sqrt{3^2 + 6^2 + 2^2} = 7$

$$(x-3)^2 + (y-6)^2 + (z-2)^2 = 49$$

5.4. $P(3, y, 2), y < 0$

$$\overline{BP} = P - B = (3, y, 2) - (6, 0, 4) = (-3, y, -2)$$

$$\sqrt{3^2 + y^2 + 2^2} = 7 \Leftrightarrow y^2 = 36 \underset{y < 0}{\Leftrightarrow} y = -6$$